

Appendix to “A Common Framework for Linear and Cyclic Multiple Sequence Alignment Problem”

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1 Test instances and optimal alignments

Instance 1

3 sequences of length 10

```
>a
CGGCAUCGGC
(([[.])])
>b
CGACCUCGGG
((.[[.])])
>c
GCGCUGACGC
(([[.].])])
```

Optimal alignment

```
a      CG-GCAUC-GGC
a      ((-[[.]-])])
b      CGACC-UC-GGG
b      ((.[[-.]-])])
c      GC-GC-UGACGC
c      ((-[[[-.].])])
```

Instance 1R

3 circular sequences of length 10; sequences of instance 1 circularized and cut at non-homologous positions

```
>a
CGGCAUCGGC
(([[.])])
>b
```

```

ACCUCGGGCG
.[[.(([]))
>c
UGACGCGCGC
.(.([]))]]

```

Optimal circular alignment, which was found in our experiment within the time limit. (By design this is equivalent to the optimal solution of instance 1.)

```

a      CG-GCAUC-GGC
a      ((-[.[.]-])]]
b      CGACC-UC-GGG
b      ((.[[-.]-])]]
c      GC-GC-UGACGC
c      ((-[[-.].])]]

```

1.1 Instance 2

3 sequences of length 15

```

>a
CGGCAAAGCCGGCGC
(((.[...{}])))]}]
>b
CGGCACGACGUGCCG
(((.[{}].)])]}]
>c
GGUCGUGCACCCGGC
((.[[{}].)])]}]

```

Optimal alignment

```

a      CG-GCAAAGC-CG-GCGC
a      ((-[...{}-)])]}]
b      CG-GC-A-CGACGUGCCG
b      ((-[[-.-{}].)])]}]
c      GGUCG-U-GCACC-CGGC
c      ((.[[-.-{}-)])]}]

```

1.2 Instance 3

3 sequences of length 20

```

>a
CGCGCGAAAGCCGCGGAGC
(((([[...{}])))]].}]
>b
CGCGCGACGACGUGCGCGA

```

```

(((([[[. {(.)})) .]]]}) .
>c
AGGGUCGCUAGCACCCGCGGC
.(((. [[[. {(.)}))]]]})

```

Optimal alignment

```

a      -CGC-GCGAAAGC-CGC-GCGAGC-
a      -(((-[[[. . {(-)})) -]]] .})-
b      -CGC-GCG--ACGACGCUGCG-CGA
b      -(((-[[-. {(.)})) .]]] -}) .
c      AGGGUCGCU-AGCACCC-GCG-GC-
c      .(((. [[[. -. {(.)})) -]]] -})-

```

1.3 Instance 4

4 Sequences of length 10

```

>a
CGGCAUCGGC
(([[. .)])]
>b
CGACCUCGGG
((. [[.)])]
>c
GCGCUGACGC
((( [. . .)])]
>d
CGGGACGAGG
((( [. . .)])]

```

Optimal alignment

```

a      CG-GCAUC-G-GC
a      ((-[ [. . ] -]) -])
b      CGACC-UC-G-GG
b      ((. [[- . ] -]) -])
c      GC-GC-UGAC-GC
c      ((-[ [- . . ] -]) -])
d      CG-GGA-C-GAGG
d      ((-[ [- . ] -]) -])

```

1.4 Instance 4R

4 circular sequences of length 10; sequences of instance 4 circularized and cut at non-homologous positions

```

>a
CGGCAUCGGC
(([[[. .)]]])
>b
ACCUCGGGCG
.[[. ([])]
>c
UGACGCGCGC
.([([[]]))]
>d
GAGGCGGGAC
([[]]([].))

```

Optimal alignment (identical to optimal alignment of Instance 4)

```

a      CG-GCAUC-G-GC
a      ((-[ [. .)-]-])
b      CGACC-UC-G-GG
b      ((.[ [-. ))-]-])
c      GC-GC-UGAC-GC
c      ((-[ [-. . ))-]-])
d      CG-GGA-C-GAGG
d      ((-[ [-. -)-].])

```