

Grundlagen der Systembiologie und der Modellierung epigenetischer Prozesse

Sonja J. Prohaska

Bioinformatics Group
Institute of Computer Science
University of Leipzig

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Genome-scale *in silico* Model

- ▶ functional *-omics* = annotating *-omics* data
- ▶ integrating *-omics* data of different kinds = systems biology
- ▶ Represent biological systems by networks.
- ▶ “*-omics*” data provide information about network components and their interactions.

Genome-scale *in silico* Model

1. Genome Sequence



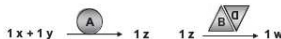
2. Genome annotation



3. 'OMICS' data integration



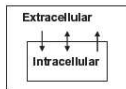
4. Network reconstruction



5. Stoichiometric representation

$$S = \begin{matrix} & \begin{matrix} A \\ B \\ C \\ D \end{matrix} & \begin{matrix} x \\ y \\ z \\ w \end{matrix} \\ \begin{matrix} A \\ B \\ C \\ D \end{matrix} & \begin{bmatrix} 1 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix} & \begin{matrix} x \\ y \\ z \\ w \end{matrix} \end{matrix}$$

6. Systems Boundaries



7. Constraints

Balances

Mass
Energy
Solvent capacity

$$S \cdot v = 0$$

$$\Delta E = 0$$

$$\sum_i c_i \leq c_{max}$$

Bounds

Thermodynamics
Enzyme/transporter capacity
Non-linear P/C phenomena

$$0 \leq v_i \leq \infty$$

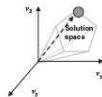
$$\alpha_j \leq v_j \leq \beta_j$$

$$\pi = RT \left(\frac{c}{M_i} + Bc^2 + \dots \right)$$

8. Steady-State Model



9. Optimal Steady-State Solution



The Cell as a Chemical Reaction Network

3. get the **nodes of the network** and integrate
 - ▶ (functional) genomics → all functional elements (mainly protein genes) that could be found and annotated in the genome
 - ▶ metabolomics → all metabolites present in a cell (substrates, cofactors, byproducts, etc. of chemical reactions)
 - ▶ proteomics → all structural proteins and enzymes (catalysts of chemical reactions) present in a cell
 - ▶ fluxomics → flows and reaction rates of all chemical reactions in a cell

The Cell as a Chemical Reaction Network

4. get the **edges of the network** by representing the chemical reactions
 - ▶ allow chemical reactions forming or breaking covalent bonds
 - ▶ allow chemical reactions that cause association or dissociation of molecules
5. get the **stoichiometry** of the chemical reactions right
 - ▶ balance atom composition (and mass)
 - ▶ invariant between organisms, independent of changes to conditions
- ▶ get the **thermodynamics** of the chemical reactions right
 - ▶ balance energy, derive relative rates of reactions
 - ▶ dependent on changes to (physiological) conditions
 - ▶ sequence alteration in binding surfaces can alter the thermodynamics of molecule association in different species
- ▶ get **direction and absolute rate** of reactions
 - ▶ determined by **enzymes** and their activity

The Cell as a Chemical Reaction Network

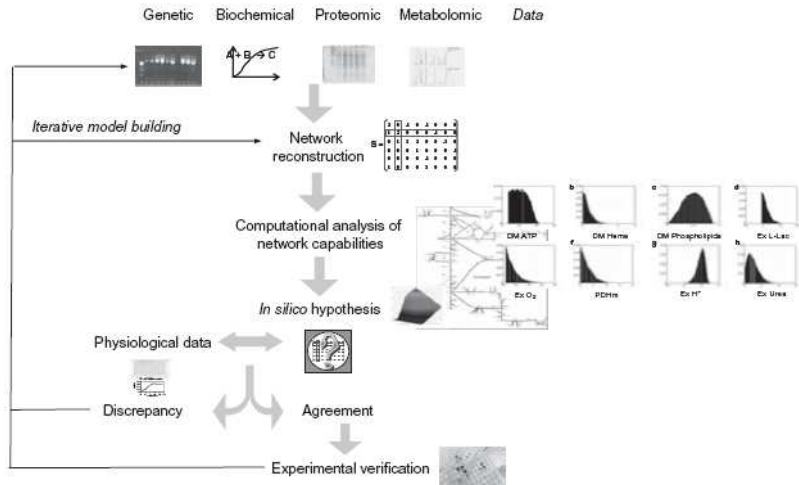
Stady-State Networks

- ▶ biological systems exist in a stady state (rather than in equilibrium)
- 6. **boundaries** for (Sub-)systems need to be defined
- 8. a network is in stady-state if the in-flow is equal to the out-flow (i.e. no accumulation or depletion of molecules occurs)

The Iterative Process of Network Reconstruction

1. identify **relevant metabolic genes** from genome annotation
2. translate gene functions into **balanced chemical reactions**
3. **network assembly** from individual reactions
4. problem of incomplete data: **fill in missing reactions** to satisfy steady-state assumption
5. **test** the model *in silico* and compare results with physiological data
6. use gene essentiality data to validate reconstruction
7. **refine iteratively**

The Iterative Process of Network Reconstruction



Formulating Biochemical Reactions

		Fumarate Reductase			
		Primary metabolites		Coenzymes	
First step	Substrate specificity	FUM	SUCC	MQNH ₂	MQN
Second step	Neutral Formulae	C ₄ H ₄ O ₄	C ₄ H ₄ O ₄	C ₂₁ H ₂₇ O ₂	C ₂₁ H ₂₇ O ₂
	Charged Formulae	C ₄ H ₂ O ₄ ²⁻	C ₄ H ₄ O ₄ ²⁻	C ₂₁ H ₂₇ O ₂ ⁰	C ₂₁ H ₂₇ O ₂ ⁰
Third step	Stoichiometry	1 FUM + 1 MQNH ₂ ? 1 SUCC + 1 MQN			
Fourth step	Directionality	1 FUM + 1 MQNH ₂ ↔ 1 SUCC + 1 MQN			
Fifth step	Localization	1 FUM [c] + 1 MQNH ₂ [c] ↔ 1 SUCC [c] + 1 MQN [c]			

Prokaryotes:

- extracellular space
- cytoplasm
- periplasm

Eukaryotes:

- extracellular space
- cytoplasm
- periplasm
- nucleus
- mitochondria
- peroxisome
- lysosome
- vacuole
- Golgi apparatus
- endoplasmatic reticulum

Constraint-based Modelling Approach

stoichiometric matrix

$$S_{mv} = \begin{pmatrix} 0 & 0 & 1 \\ 0 & -1 & -1 \\ 0 & -1 & 0 \\ -1 & 1 & 1 \\ 0 & 0 & -1 \\ 1 & 0 & 0 \end{pmatrix}$$

- ▶ while m are the metabolites, v are the fluxes/reactions
- ▶ a stoichiometric matrix S transforms the flux vector $v = (v_1, v_2, \dots, v_n)$ into a vector of time derivatives of the concentration vector $x = (x_1, x_2, \dots, x_n)$
- ▶ $\frac{dx}{dt} = Sv$, steady state balance $Sv = 0$
- ▶ $\frac{dx_i}{dt} = \sum_k S_{ik} v_k$ is the sum of all fluxes producing or consuming x_i

Constraint-based Modelling Approach

stoichiometric matrix

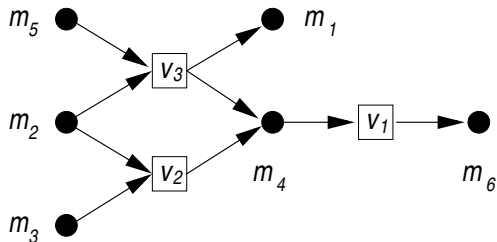
$$S_{mv} = \begin{pmatrix} 0 & 0 & 1 \\ 0 & -1 & -1 \\ 0 & -1 & 0 \\ -1 & 1 & 1 \\ 0 & 0 & -1 \\ 1 & 0 & 0 \end{pmatrix}$$

$m_1 = c_1$; $m_2 = c_2$; $m_3 = c_3$; $m_4 = c_2 c_3$; $m_5 = c_1 c_3$; $m_6 = c_3 c_2$

- ▶ reversible conversion: $c_2 c_3 \xrightarrow{v_1} c_3 c_2$
- ▶ bi-molecular association: $c_s + c_3 \xrightarrow{v_2} c_2 c_3$
- ▶ cofactor-coupled reaction: $c_2 + c_1 c_3 \xrightarrow{v_3} c_2 c_3 + c_1$ with c_1 as co-factor

Constraint-based Modelling Approach

network representation



Constraint-based Modelling Approach

- ▶ physiochemical constraints (inviolable)
 - ▶ mass, energy and momentum conserved
 - ▶ slow diffusion of macromolecules in viscous medium
 - ▶ reaction rates determined by local concentrations
 - ▶ reactions proceed in the direction of negative free-energy change
- ▶ spatial constraints
 - ▶ transport, structures
 - ▶ e.g. length, packaging and accessibility constrain arrangement of DNA
- ▶ environmental constraints
 - ▶ e.g. nutrient availability, temperature and osmolarity
 - ▶ important to determine phenotypic properties and fitness
- ▶ regulatory (self-imposed) constraints
 - ▶ allow the cell to eliminate suboptimal phenotypic states
 - ▶ e.g. transcriptional, translational, enzyme activity regulation

Given the Network...

- ▶ sample the network and study **network properties**
 - ▶ population of the flux space
 - ▶ interdependencies and complexity
 - ▶ robustness to disturbance
 - ▶ flexibility to adopt to changing environments
- ▶ given an objective function linear optimization or linear programming can be used to calculate one **optimal reaction network state** (e.g. optimal growth)
- ▶ in large, more interconnected networks **alternative optima** can be examined with mixed-integer LP algorithms
- ▶ **optimize overproduction of a product**: simultaneously optimize growth and secretion of the target product by (multiple) gene deletion.

References



[Choi, 2007] Sangdun Choi. *Introduction to Systems Biology*.



[Kaneko, 2006] Kunihiko Kaneko. *Life: An Introduction to Complex Systems Biology*.